Measurement of the Near-Threshold $e^+e^- \rightarrow D^{(*)\pm}D^{(*)\mp}$ Cross Section using Initial-State Radiation


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Exclusive $e^+e^-\rightarrow D^{(*)}\bar{D}^{(*)}$ hadronic cross sections to final states with charm meson pairs are of special interest because they provide information on the spectrum of $J^{PC}=1^{--}$ charmonium states above the open-charm threshold, which is poorly understood [1]. The observation of the charmoniumlike $Y(4260)$ state, seen only in $J/\psi\pi\pi(K\bar{K})$ final states [2–5], has stimulated renewed interest in this field. Curiously, the $Y(4260)$ peak position is close to a local minimum of the total hadronic cross section [6]. The large branching fraction to $J/\psi\pi\pi$ inferred from the total hadronic cross section is unexpected for a conventional charmonium state with such a large mass and width. In a recent measurement [7] the $e^+e^-\rightarrow D\bar{D}$ cross section is described by known charmonium states without a significant $Y(4260)$ contribution. A study of the production cross section of the charmed meson pairs in this energy range could help clarify this intriguing situation.

In this Letter we report a measurement of exclusive cross sections for $e^+e^-\rightarrow D^{(*)}\bar{D}^{(*)}$ and $e^+e^-\rightarrow D^+\bar{D}^-$ [8] using initial-state radiation (ISR). The data used for this analysis correspond to an integrated luminosity of 547.8 fb$^{-1}$ collected with the Belle detector [9] at the $\Upsilon(4S)$ resonance and nearby continuum at the KEKB asymmetric-energy $e^+e^-$ collider [10].

To measure the $e^+e^-$ hadronic cross section at $\sqrt{s}$ smaller than the initial $e^+e^-$ center-of-mass (c.m.) energy ($E_{c.m.}$) at $B$ factories, ISR can be used [11]. ISR allows a measurement of cross sections in a broad energy range while the high luminosity of the $B$ factories compensates for the suppression associated with the emission of a hard photon. The selection of $e^+e^-\rightarrow D^{(*)}\gamma_{isr}$ signal events using full reconstruction of both the $D^{(*)}$ and $D^-$ mesons, plus the $\gamma_{isr}$ photon, suffers from low efficiency due to the low $D^{(*)}$ reconstruction efficiencies, small branching fractions, and the low geometrical acceptance for the $\gamma_{isr}$, which tends to be emitted along the beam line. Here, we use a method that achieves higher efficiency by requiring full reconstruction of only one of the $D^{(*)}$ mesons, the $\gamma_{isr}$, and the slow $\pi_{slow}$ from the other $D^{(*)}$. In this case the spectrum of masses recoiling against the $D^{(*)}\gamma_{isr}$ system:

$$M_{rec}(D^{(*)}\gamma_{isr}) = \sqrt{(E_{c.m.} - E_{D^{(*)}\gamma_{isr}})^2 - p_{D^{(*)}\gamma_{isr}}^2}$$  

peaks at the $D^{(*)}$ mass. Here $E_{D^{(*)}\gamma_{isr}}$ and $p_{D^{(*)}\gamma_{isr}}$ are the c.m. energy and momentum, respectively, of the $D^{(*)}\gamma_{isr}$ combination. This peak is expected to be wide and asymmetric due to the photon energy resolution and higher-order corrections to ISR. From the Monte Carlo (MC) simulation the resolution of this peak is estimated to be $\sim300$ MeV/c$^2$, which is not sufficient to separate the $D\bar{D}^*$, $D^*\bar{D}^*$, or $D^{(*)}\bar{D}^{(*)}\pi$ final states. To disentangle the contributions from these final states and to suppress combinatorial backgrounds, we use the slow pion from the unreconstructed $D^-$. The difference between the mass recoiling against $D^{(*)}\gamma_{isr}$ and $D^{(*)}\pi_{slow}\gamma_{isr}$ (recoil mass difference):

$$\Delta M_{rec} = M_{rec}(D^{(*)}\gamma_{isr}) - M_{rec}(D^{(*)}\pi_{slow}\gamma_{isr})$$  

(2)
has a narrow distribution ($\sigma \sim 1.4 \text{ MeV}/c^2$) around the nominal $m_{D^-} - m_{\bar{p}}$, since the uncertainty in $\gamma_{\text{ ISR}}$ momentum partially cancels out.

For the measurement of the exclusive cross section, one needs to determine the $D^{(*)+}D^{*-}$ mass when one of the $D^{*}$’s is not reconstructed. In the absence of higher-order QED processes, $M(D^{(*)+}D^{*-})$ is the mass recoiling against the $\gamma_{\text{ ISR}}$. However, the photon energy resolution results in a typical $M_{\text{rec}}(\gamma_{\text{ ISR}})$ resolution of ~100 MeV, which is too wide for the study of relatively narrow $D^{(*)+}D^{*-}$ mass states. We significantly improve the $M_{\text{rec}}(\gamma_{\text{ ISR}})$ resolution by applying a refit that constrains $M_{\text{rec}}(D^{(*)+}\gamma_{\text{ ISR}})$ to the nominal $D^{*-}$ mass. In this way we use the well-measured properties of the fully reconstructed $D^{(*)+}$ to correct the energy of the $\gamma_{\text{ ISR}}$. As a result, the $M_{D^{(*)+}}(D^{*-})$ resolution is improved by a factor of ~10 and varies from ~6 MeV/$c^2$ around threshold to ~12 MeV/$c^2$ at $M_{D^{(*)+}}D^{*-} = 5.0$ GeV/$c^2$. The recoil mass difference after the refit procedure ($\Delta M_{\text{rec}}$) has a resolution by a factor of ~2. Finally, the cross section is derived from the $D^{(*)+}D^{*-}$ mass spectrum after the refit.

All charged tracks should originate from the interaction point (IP) with the requirements $dr < 2$ cm and $dz < 4$ cm, where $dr$ and $dz$ are the impact parameters perpendicular to and along the beam direction with respect to the IP. Charged kaons are required to have the ratio of particle identification likelihoods, $P_K = L_K/(L_K + L_{\pi})$ [12], larger than 0.6. No identification requirements are applied for pion candidates. $K_S^0$ candidates are reconstructed by combining $\pi^+\pi^-$ pairs with an invariant mass within 10 MeV/$c^2$ of the nominal $K_S^0$ mass. The distance between the two pion tracks at the $K_S^0$ vertex must be less than 1 cm, the transverse flight distance from the interaction point is required to be greater than 0.1 cm, and the angle between the $K_S^0$ momentum direction and the flight direction in the $x$-$y$ plane should be smaller than 0.1 rad. Photons are reconstructed in the electromagnetic calorimeter as showers with energies greater than 50 MeV that are not associated with charged tracks. ISR photon candidates are required to have energies greater than 2.5 GeV. Pairs of photons are combined to form $\pi^0$ candidates. If the mass of a $\gamma\gamma$ pair lies within 15 MeV/$c^2$ of the nominal $\pi^0$ mass, the pair is fit with a $\pi^0$ mass constraint and considered as a $\pi^0$ candidate. $D^0$ candidates are reconstructed using five decay modes: $K^-\pi^+$, $K^-\pi^+$, $K^-\pi^+\pi^-$, $K_S^0\pi^-\pi^-$, and $K^-\pi^+\pi^0$. A ±15 MeV/$c^2$ mass window is used for all modes except for $K^-\pi^+\pi^+$, where a ±10 MeV/$c^2$ requirement is applied (~2.5$\sigma$ in each case). $D^+$ candidates are reconstructed using the decay modes $K_S^0\pi^+$, $K^-\pi^+\pi^+$, and $K^-\pi^+\pi^+$. A ±10 MeV/$c^2$ mass window is used for all $D^+$ modes. To improve the momentum resolution of $D$ meson candidates, final tracks are fitted to a common vertex applying the nominal $D^0$ or $D^+$ mass as a constraint. $D^0$ candidates are selected via $D^{*+} \rightarrow D^0\pi^+$ and $D^{+} \rightarrow D^0\pi^0$ decay modes with a ±2 MeV/$c^2$ $D^* - D$ mass-difference window. A mass- and vertex-constrained fit is also applied to $D^*$ candidates.

The distribution of $M_{\text{rec}}(D^{*+}\gamma_{\text{ ISR}})$ mass in the data, without any requirements on the slow pion, is shown in Fig. 1(a). The excess around the $D^{*-}$ mass includes the $e^+e^- \rightarrow D^{*+}D^{*-}\gamma_{\text{ ISR}}$ signal as well as contributions from the $e^+e^- \rightarrow D^{*+}\gamma_{\text{ ISR}}$ channel. The shoulder at higher masses is due to $e^+e^- \rightarrow D^{*+}D^{0}\pi\gamma_{\text{ ISR}}$. The excess that is evident at ~2.5 GeV/$c^2$ corresponds to $e^+e^- \rightarrow D^{*+}D^{*-}\gamma_{\text{ ISR}}$ channel. The background from the other processes is substantially suppressed by the inclusion of the slow pion from the unreconstructed $D^{*-}$ and the tight requirement on $\Delta M_{\text{fit}}$; i.e., within ±2 MeV/$c^2$ of the nominal $m_{D^-} - m_{\bar{p}}$, a clean peak corresponding to $e^+e^- \rightarrow D^{*+}D^{*-}$ is evident in the $M_{\text{rec}}(D^{*+}\gamma_{\text{ ISR}})$ distribution [Fig. 1(b)]. We define the signal region by the requirement that $M_{\text{rec}}(D^{*+}\gamma_{\text{ ISR}})$ be within ±0.2 GeV/$c^2$ of the nominal $D^{*-}$ mass. This tight requirement suppresses $e^+e^- \rightarrow D^{*+}D^{*-}\pi\gamma_{\text{ ISR}}$ events, which have a similar $\Delta M_{\text{fit}}$ distribution. The spectrum of $\Delta M_{\text{rec}}$ for the signal $M_{\text{rec}}(D^{*+}\gamma_{\text{ ISR}})$ window after the refit procedure in data is shown in Fig. 1(c).

In case of multiple entries, the $D^{*+}\pi$ candidate with the minimum value of $\chi^2_{\text{tot}} = \chi^2_{M(D^0)} + \chi^2_{M(D^{*+})} + \chi^2_{\Delta M_{\text{rec}}}$ is chosen, where each $\chi^2$ is defined as the squared ratio of the
deviation of the measured parameter from the expected signal value and the corresponding resolution.

The following sources of background are considered: (1) combinatorial background under the reconstructed $D^{+}$ peak; (2) real $D^{+}$ mesons coming from the signal or other processes combined with a combinatorial slow pion; (3) both the $D^{+}$ and slow pion are combinatorial; (4) the reflection from the process $e^{+}e^{-} \rightarrow D^{0}\bar{D}^{0}\pi^{0}\gamma_{\text{isr}}$ with an extra $\pi^{0}$ in the final state; (5) the contribution of $e^{+}e^{-} \rightarrow D^{0}\bar{D}^{0}\pi^{0}$ when an energetic $\pi^{0}$ is misidentified as a single $\gamma_{\text{isr}}$. The contributions of backgrounds (1) and (2) are extracted using $D^{0}$ and $\Delta M_{\text{fit}}$ sidebands, which have twice the area of the signal region. The latter sideband is shifted by 10 MeV/c² from the signal region to avoid signal oversubtraction due to the higher-order ISR tail. Background (3) is present in both the $M(D^{0})$ and $\Delta M_{\text{fit}}$ sidebands and is, thus, subtracted twice. To account for this oversubtraction we use a two-dimensional sideband region, where events are selected from both the $D^{0}$ and the $\Delta M_{\text{fit}}$ sidebands. The total fraction of backgrounds (1)–(3), found to be as large as ~10%, is subtracted from the signal-region $D^{+}\bar{D}^{0}$ mass spectrum. Process (4) produces a broad peak in the $\Delta M_{\text{rec}}$ distribution around the nominal $m_{D^{0}} - m_{\pi^{0}}$ value and, thus, is not contained in the $\Delta M_{\text{rec}}$ sidebands. The dominant part of this background is suppressed by the tight requirement on $M_{\text{rec}}(D^{0}\gamma_{\text{isr}})$. The remaining part is estimated by applying a similar partial reconstruction method to the isospin-conjugate process $e^{+}e^{-} \rightarrow D^{0}\bar{D}^{0}\pi^{0}\gamma_{\text{isr}}$: a $D^{0}$ is fully reconstructed and the slow pion from a $D^{0}$ is used for the $\Delta M_{\text{fit}}$ requirement. Since there is a charge imbalance in this final state, only events with a missing extra $\pi^{0}$ can contribute to the $\Delta M_{\text{fit}}$ peak. To extract the level of background (4), this spectrum is rescaled according to the ratio of $D^{0}$ and $D^{+}$ reconstruction efficiencies and an isospin factor of $\frac{1}{2}$. The contribution from background (4) is found to be consistent with zero. Uncertainties in this estimate are included in the systematic error. The contribution of background (5) is determined from reconstructed $e^{+}e^{-} \rightarrow D^{+}\bar{D}^{0}\pi^{0}$ events using a similar partial reconstruction technique but with an energetic $\pi^{0}$ replacing the $\gamma_{\text{isr}}$. The contribution of this background is found to be negligible small; uncertainties in this estimate are also included in the systematic error.

The analysis of the $e^{+}e^{-} \rightarrow D^{+}\bar{D}^{0}$ cross section is identical to that described above for $e^{+}e^{-} \rightarrow D^{+}\bar{D}^{+}$ with the fully reconstructed $D^{+}$ meson replaced by a fully reconstructed $D^{0}$ meson. The distribution of $M_{\text{rec}}(D^{0}\gamma_{\text{isr}})$ with no requirements on the slow pion from the $D^{0}$ is shown in Fig. 1(d). The excess around the nominal $D^{0}$ mass corresponds to the $e^{+}e^{-} \rightarrow D^{0}\bar{D}^{0}\gamma_{\text{isr}}$ signal plus overlaps from the $e^{+}e^{-} \rightarrow D^{+}\bar{D}^{+}\gamma_{\text{isr}}$ channel. The shoulder at higher masses is due to $e^{+}e^{-} \rightarrow D^{0}D^{0}\gamma_{\text{isr}}$. The requirement of a detected slow pion from the unreconstructed $D^{0}$ and a tight requirement on $\Delta M_{\text{fit}}$ provides the clean $e^{+}e^{-} \rightarrow D^{+}\bar{D}^{0}$ signal peak in the distribution of $M_{\text{rec}}(D^{+}\gamma_{\text{isr}})$ that is shown in Fig. 1(e).

The $\Delta M_{\text{fit}}$ distribution for the signal $M_{\text{rec}}(D^{+}\gamma_{\text{isr}})$ window is shown in Fig. 1(f). In the case of multiple entries, we apply a single candidate selection procedure similar to that used for $D^{+}D^{0}$ to all the distributions shown below.

Similar sources of background (1)–(5) are considered for the $e^{+}e^{-} \rightarrow D^{+}\bar{D}^{0}$ study. The contributions of backgrounds (1)–(3) are determined using $D^{+}$ and $\Delta M_{\text{fit}}$ sidebands with twice the area of the signal region. Here again, background (3) is present in both $M(D^{+})$ and $\Delta M_{\text{fit}}$ sidebands and thus subtracted twice. To account for this oversubtraction we use a two-dimensional sideband region that contains pure background (3) events. The level of contamination from background (4) is determined from isospin-conjugate events, $e^{+}e^{-} \rightarrow D^{0}\bar{D}^{0}\pi^{0}\gamma_{\text{isr}}$ in the data. The $D^{0}\bar{D}^{0}$ analysis is repeated with the fully reconstructed $D^{0}$'s replaced by fully reconstructed $D^{0}$'s. The $D^{0}\bar{D}^{0}$ mass distribution, after combinatorial background subtraction, is rescaled according to the ratio of $D^{0}$ and $D^{0}$ reconstruction efficiencies and an isospin factor of $\frac{1}{2}$. By chance, the contamination from the process $e^{+}e^{-} \rightarrow D^{+}\bar{D}^{0}\pi^{0}$ followed by $D^{0} \rightarrow D^{+}\pi^{0}$ is also included in our estimate with correct scaling because $B(D^{+} \rightarrow D^{0}\pi^{0})/B(D^{0} \rightarrow D^{+}\pi^{0})$ is also ~1. The contribution from background (5) determined from reconstructed $e^{+}e^{-} \rightarrow D^{0}\bar{D}^{0}\pi^{0}$ events in the data is found to be negligibly small and taken into account in the systematic error. The total background level is ~20% or less of the signal for all values of $M(D^{+}\bar{D}^{0})$.

The $e^{+}e^{-} \rightarrow D^{0}\bar{D}^{0}$ cross sections are extracted from the $D^{0}\bar{D}^{0}$ mass distributions [13]

$$\sigma(e^{+}e^{-} \rightarrow D^{0}\bar{D}^{0}) = \frac{dN/dm}{n_{\text{tot}}dL/dm},$$

where $m \equiv M(D^{0}\bar{D}^{0})$, $dN/dm$ is the mass spectra obtained before corrections for resolution and higher-order radiation, while $n_{\text{tot}}$ is the total efficiency. The factor $dL/dm$ is the differential ISR luminosity

$$dL/dm = \frac{\alpha}{\pi x} \left( 2 - 2x + x^2 \right) \ln \frac{1 + C}{1 - C} - x^2 C \frac{2m\mathcal{L}}{E_{\text{c.m.}}^2},$$

where $x = 1 - m^2/E_{\text{c.m.}}^2$, $\mathcal{L}$ is the total integrated luminosity, and $C = \cos \theta_{0}$, where $\theta_{0}$ defines the polar angle range for $\gamma_{\text{isr}}$ in the $e^{+}e^{-}$ c.m. frame: $\theta_{0} < \theta_{\gamma_{\text{isr}}} < 180^\circ - \theta_{0}$. The reconstruction efficiencies, determined as a function of $M(D^{0}\bar{D}^{0})$ by MC simulation, are found to be independent of $M(D^{0}\bar{D}^{0})$ for both processes and are equal to $\eta(D^{0}\bar{D}^{0}) = 4.3 \times 10^{-3}$ and $\eta(D^{+}\bar{D}^{0}) = 3.9 \times 10^{-3}$. The resulting exclusive $e^{+}e^{-} \rightarrow D^{0}\bar{D}^{0}$ cross sections are shown in Fig. 2 with statistical uncertainties only. Since the bin width is much larger than the resolution, no correction for resolution is applied. Since a
reliable fit to the cross sections obtained above requires a solution to a nontrivial and model-dependent problem of coupled channels and threshold effects, we do not report results here.

The systematic errors for the $\sigma(e^+e^-\rightarrow D^{(*)+}D^{(*)-})$ measurements are summarized in Table I. The systematic errors associated with the background (1)–(3) subtraction are estimated to be 3% from the uncertainty in the scaling factors for the sideband subtractions using fits to the $M(D^{(*)+})$ and $\Delta M_{\text{rec}}^{\text{mu}}$ distributions in the data with different signal and background parametrization. Uncertainties in backgrounds (4)–(5) are estimated conservatively to be smaller than 2% of the signal in the case of $D^{(*)+}D^{(*)-}$; these two sources are added linearly to give 5% in total. In the case of the $D^+D^{*-}$, backgrounds (4)–(5) are subtracted using the data and only the uncertainty in the scaling factor for the subtracted distribution is taken into account. A second source of systematic error is due to the unknown helicity angle composition of the $D^+D^{*-}$ final state which can be a mixture of $D_L^{+}D_L^{*-}$, $D_T^{+}D_T^{*-}$, and $D_L^{+}D_T^{*-}$, where the subscripts $L$ and $T$ refer to longitudinally and transversely polarized $D^{(*)}$’s. For the efficiency calculation, we assume equal fractions of these helicity states and consider the extreme cases (pure $D_L^{+}D_L^{*-}$ and pure $D_T^{+}D_T^{*-}$) for the efficiency uncertainty. There is no corresponding uncertainty in the case of the $D^0D^{*-}$ final state, where the $D^{*-}$ polarization is fixed by angular momentum and parity conservation. A third source of systematic error comes from the uncertainties in track and photon reconstruction efficiencies, which are 1% per track, 2% per slow pion, and 1.5% per photon, respectively. The systematic error ascribed to the cross-section calculation is estimated from a study of the $C$ dependence of the final result and includes a 1.5% error on the total luminosity. Other contributions come from the uncertainty in the identification efficiency and the absolute $D^0$ and $D^{(*)+}$ branching fractions [14].

In summary, we report the first measurements of exclusive $e^+e^-\rightarrow D^{(*)+}D^{(*)-}$ and $e^+e^-\rightarrow D^*+D^*$ cross sections at $\sqrt{s}$ around the $D^{(*)+}D^{(*)-}$ and $D^*+D^*$ thresholds with initial-state radiation. The shape of the $e^+e^-\rightarrow D^{(*)+}D^{(*)-}$ cross section is complicated with several local maxima and minima. The minimum near 4.25 GeV/$c^2$—in the $Y(4260)$ region—could be due to $D_L^{+}D_L^{*-}$ ($D^{(*)*}$) threshold effects described in [15–17] or due to destructive interference of this state with other $\psi(nS)$ states. Aside from a prominent excess near the $\psi(4040)$, the $e^+e^-\rightarrow D^{(*)+}D^{(*)-}$ cross section is relatively featureless. The measured cross sections are compatible [18] within errors with the $D^{(*)+}D^*$ exclusive cross section in the energy region up to 4.260 GeV measured by CLEO-c [19].

We thank the KEKB group for excellent operation of the accelerator, the KEK cryogenics group for efficient sole-

![FIG. 2. The exclusive cross sections for (a) $e^+e^-\rightarrow D^{(*)+}D^{(*)-}$ and (b) $e^+e^-\rightarrow D^+D^*$.](https://example.com/figure2.png)

**TABLE I.** The systematic errors for cross sections [%].

<table>
<thead>
<tr>
<th>Source</th>
<th>$D^{(<em>)+}D^{(</em>)-}$</th>
<th>$D^{(<em>)+}D^{(</em>)-}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Background subtraction</td>
<td>±5</td>
<td>±4</td>
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<tr>
<td>Angular distributions</td>
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<td>±5</td>
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<tr>
<td>Reconstruction</td>
<td>±7</td>
<td>±6</td>
</tr>
<tr>
<td>Cross section calculation</td>
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<td>±2</td>
</tr>
<tr>
<td>$\mathcal{B}(D^{(*)+})$</td>
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<td>±5</td>
</tr>
<tr>
<td>MC statistics</td>
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<td>±1</td>
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<tr>
<td>Total</td>
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<td>±10</td>
</tr>
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</table>

[8] Charge-conjugate modes are included throughout this Letter.
[18] Since only charged final states are measured, our results should be scaled by a factor of 2 for this comparison.